

# Forensic Statistics

*15<sup>th</sup> International  
Symposium on  
Human Identification*

## Calculation of Mixture Statistics

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# TOPICS COVERED

- What Constitutes a DNA Mixture?
- Common Mixture Explanations
- Exclusion Probability
- Likelihood Ratio
- Examples

# What Constitutes a DNA Mixture?

- Presence of three or more alleles at several loci typed

**Rationale:** No more than two alleles can originate from a single individual (occasional exceptions do exist – e.g., Tri-allelic TPOX profiles in single individuals have been found in several populations).

# What Constitutes a DNA Mixture?

- ➔ Imbalance of Alleles detected in the sample

**Peak height difference, intensity difference, etc. are caused by differential amount of DNA contributed by different contributors in a sample.**

# What Constitutes a DNA Mixture?

## Circumstantial Evidence

**Search for foreign DNA in intimate samples, in many cases, may recover traces of DNA of the person who is technically a “substrate” even if attempts to fractionate the DNA are made during the test... incomplete differential extracts, penile swabs, etc**

# Common Mixture Interpretations

- Profiles of two or more tested persons explain all alleles detected in the mixture sample,
- Mixture contains unexplained alleles beyond the ones present in the profiles of the known persons profiled,
  - ☛ Unknown persons contributed to the mixture,
  - ☛ Contamination

# Common Mixture Interpretations

- Alleles with low intensity consistently belong to specific (known or unknown) persons profiled (i.e., minor and major contributors in the DNA mixture).

# Mixture Interpretation

Alleles that enter into statistical calculations first meet the interpretation guidelines for data analysis

- RFU Threshold
- Peak ratios/percent stutter
- "Match" criteria



But, before we begin...

Calculations based on mixed profiles fall under the same statistical assumptions that we use in the calculation of single source profile statistics

# Assumptions

- ☛ Hardy Weinberg Equilibrium
- ☛ No allele dropout
- ☛ Individuals are unrelated
- ☛ Population substructure is negligible
- ☛ Contributors are of the same race

But also,  
unlike conventional frequency  
reporting...

We have to address specific hypotheses

## Two common questions are generally asked:

- How often would a random person be excluded as a contributor to the observed mixture? (**Exclusion Probability**)
- What statistical support is there for any postulated hypothesis of the origin of the mixture? (**Likelihood**)

# Exclusion Probability

Exclusion probability addresses the question:

How often a random person would have been excluded as a contributor in the observed DNA mixture?

# Exclusion Probability

- This is a measure of how **powerful** the DNA testing panel is in excluding noncontributory individuals from the analysis
- The statistic is based on the **allelic composition** of the mixture...**not** the profiles of potential **contributors**

# Exclusion Probability

The computation of the **exclusion probability** is done exactly as in the parentage testing

# Exclusion Probability

For example:

Suppose that the mixture contains  $i$  alleles ( $A_1, A_2, \dots, A_i$  at a locus),

whose frequencies are  
 $p_1, p_2, \dots, p_i$  respectively)

# Exclusion Probability

Individuals whose genotypes contain only one or two of the  $i$  alleles **cannot** be excluded as contributors in this mixture.

To be excluded, the person should have at least one allele in his/her genotype not seen in the mixture.



# Exclusion Probability

The probability of **inclusion** is given by

$$(p_1 + p_2 + \dots + p_i)^2$$

and

# Exclusion Probability

The compliment of *Inclusion Probability* defines the  
**Exclusion Probability**

$$PE = 1 - (p_1 + p_2 + \dots + p_i)^2$$

Also

# Exclusion Probability

In presence of departure from HWE,  
 $PE_i$  can be computed as

$$PE_i = 1 - [p^2 + \theta p(1 - p)]$$

where  $p = p_1 + p_2 + \dots + p_i$ , and  
 $\theta$  = the population substructure  
parameter for adjustment of  
allelic dependence.

# Exclusion Probability

When multiple loci are typed, the combined Probability of Exclusion can be computed as

$$PE_{TOT} = 1 - [(1 - PE_1) \times (1 - PE_2) \times \dots \times (1 - PE_i)]$$

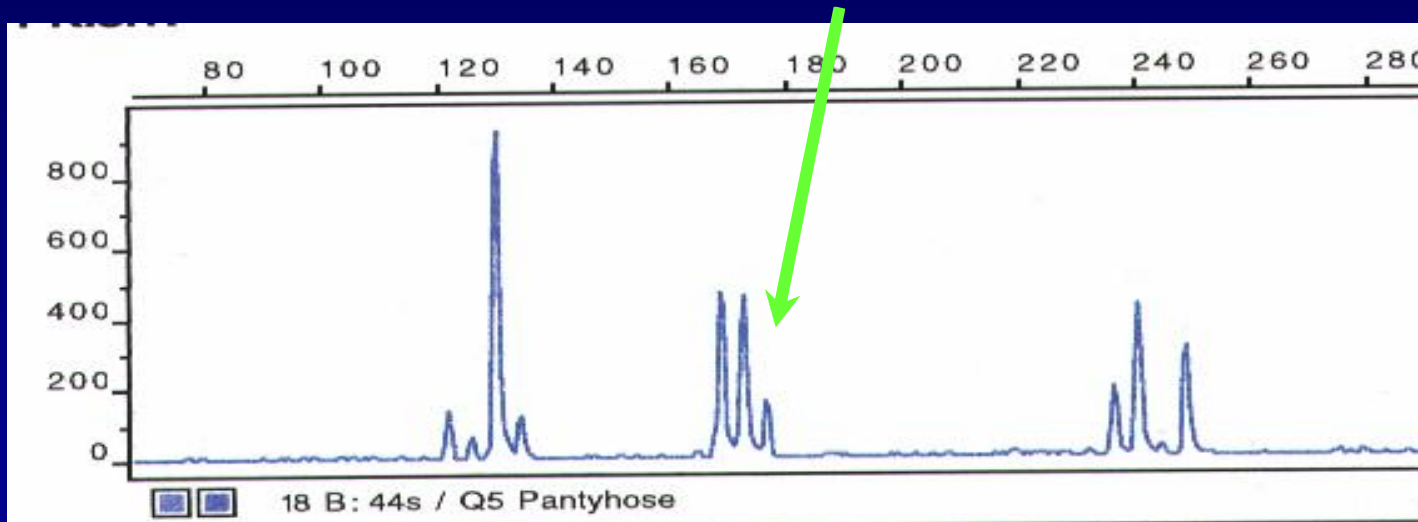
# Exclusion Probability

What does this actually tell us???

- ➡ Statistical robustness of the testing panel
- ➡ Whether the statistical support for any given hypothesis of mixture origin is conservative

## How about an example...

A mixture sample shows alleles 7, 8, and 9 at the THO1 locus.



The evidence is from a semen stain found inside the pantyhose of a victim who claimed to have been raped.

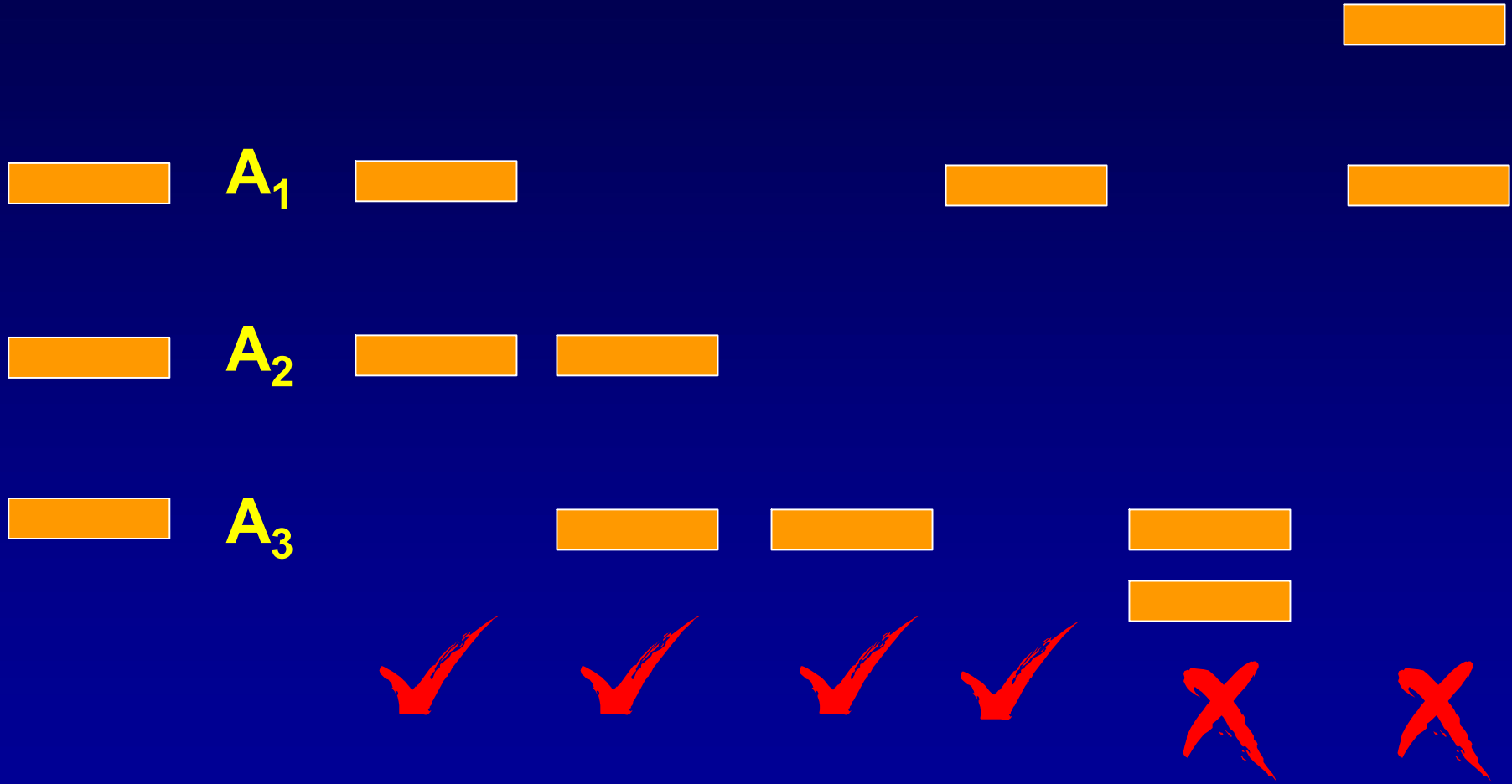
We have the following data:

<b>Mixture Alleles</b>	...	<b>7, 8, 9</b>
<b>Victim Alleles</b>	...	<b>8, 9</b>
<b>Suspect Alleles</b>	...	<b>7, 8</b>

Neither the suspect nor the victim can be excluded as part contributors in the DNA of the mixture

**But, who else can?**

# Evidence





Given that both victim and suspect are of the same race:

frequencies of the alleles are:

$$p_7 = 0.1, p_8 = 0.2, \text{ and } p_9 = 0.3$$

**Exclusion Probability** would be

$$\begin{aligned} PE &= 1 - (0.1 + 0.2 + 0.3)^2 \\ &= 0.64, \text{ or } 64\% \end{aligned}$$

# What does this mean???

64% of randomly tested persons would have been excluded as a contributor of the DNA of the mixed sample

WHY??

Says nothing about:

- ➡ Victim or suspect
- ➡ Other potential contributors
- ➡ Ratio of mixture, etc...

What if we couldn't assume H-W?

$$PE_i = 1 - [p^2 + \theta p(1 - p)]$$

$$p = p_7 + p_8 + p_9$$

$$p = 0.1 + 0.2 + 0.3 \\ = 0.6$$

Using a  $\theta = 0.01$

$$PE_i = 1 - [0.6^2 + 0.01(0.6)(1 - 0.6)] \\ = 0.6384$$

What about a  $\theta = 0.03$  ?

$$PE_{\ell} = 1 - [p^2 + \theta p(1 - p)]$$

$$p = 0.6$$

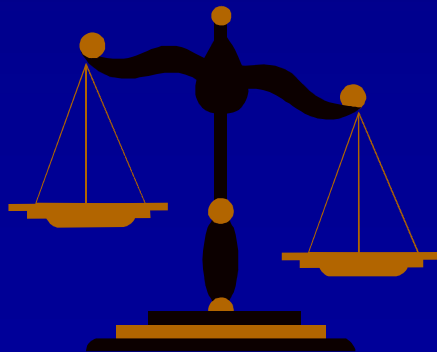
$$PE_{\ell} = 1 - [0.6^2 + 0.03(0.6)(1 - 0.6)]$$

$$= 0.6328$$

Approximately 1% change in PE

# Mixtures and Likelihood Ratios

Likelihood Ratio (LR) is a concept that compares the probabilities of a **given observation** under two mutually exclusive hypotheses.



So, now we are including a statement about the **circumstances of the case** as well as the actual profiles determined for the **victim, suspect and evidentiary sample**

However, this opens many possibilities... all of which need to be addressed!

Let's use the same example used in the Exclusion Probability calculation for our LR interpretation of a DNA mixture

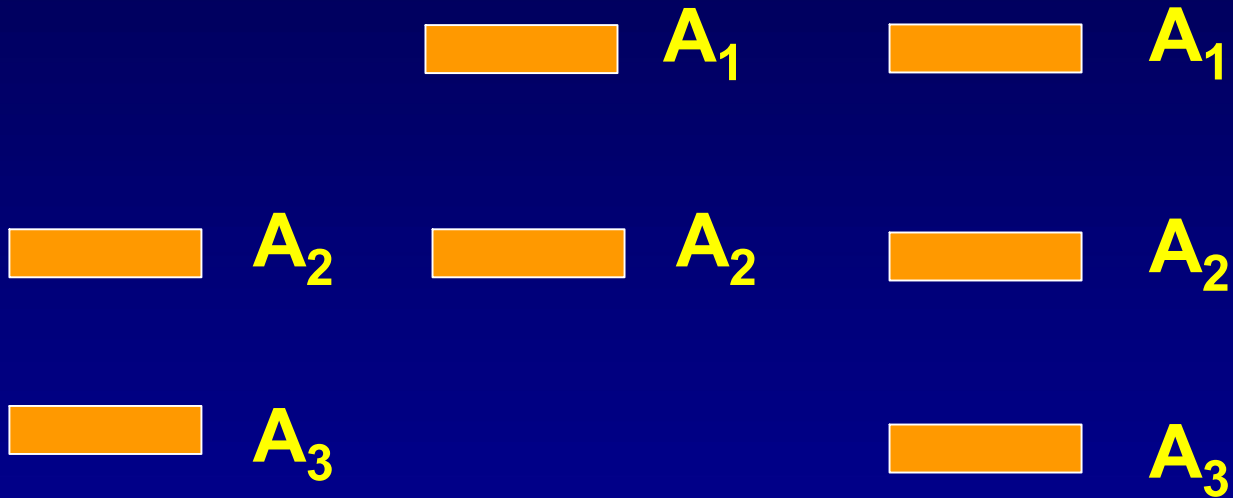
We have the following data:

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<b>Victim Alleles</b>	...	<b>8, 9</b>
<b>Suspect Alleles</b>	...	<b>7, 8</b>

**Victim**

**Suspect**

**Evidence**



**Three Allele Scenario**

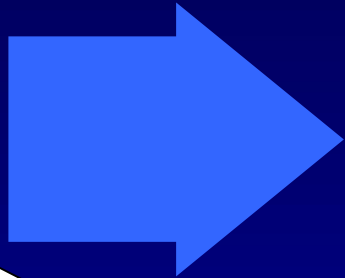
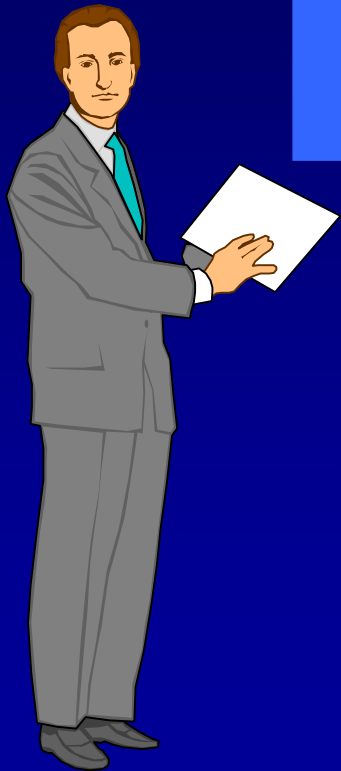


# Three Alleles

Victim is heterozygote -  $A_2A_3$

Suspect is heterozygote-  $A_1A_2$

# Mutually Exclusive Hypotheses

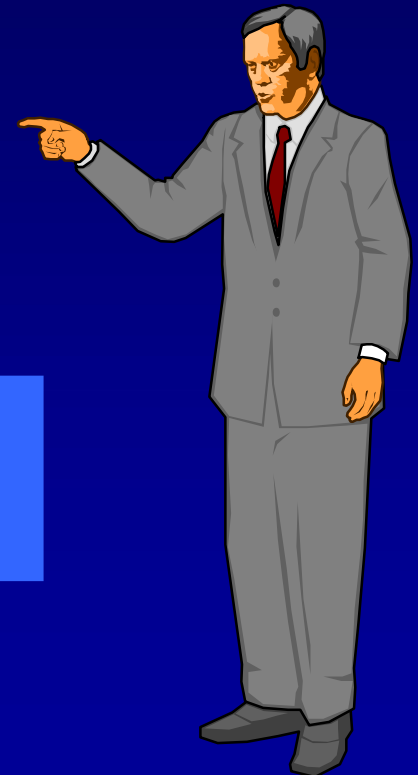
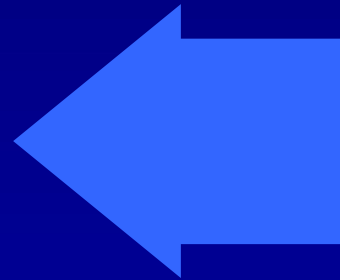


**Prosecution**

DNA is from victim  
and suspect

**Defense**

DNA is from victim  
and unknown person



The prosecution may postulate that the victim and the suspect together explain **all** alleles seen in the mixture.

$H_0$ : The mixture originated from the epithelial cells of the victim and the semen of the suspect

Under this hypothesis,

the only **possible** mixture profile  
is 7,8,9

and thus the mixture observation  
is **explained** with a probability of  
**100%**.

**BUT...**

The defense might argue that the following two alternative hypotheses should also be entertained:

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$H_1$ : The mixture originated from the victim and an unknown person,

The defense might argue that the following two alternative hypotheses should also be entertained:

$H_1$ : The mixture originated from the victim and an unknown person,

and

$H_2$ : The mixture originated from two unknown persons

Let's tackle the first scenario:

So, the **Likelihood** according to the prosecution's hypothesis ( $H_0$ ) is **1**

We need to calculate the likelihood according to the defense hypothesis 1...



Since the victim has the profile (8,9), the **unknown** person can have **three possible genotypes**:

(7,7), (7,8), or (7,9),

which would explain all alleles in the mixture, in combination with the victim.

Using our allele frequencies from before:

$$p_7 = 0.1, p_8 = 0.2, \text{ and } p_9 = 0.3$$

the probability of observing the mixture profile under the defense hypothesis  $H_1$  is:

$$L_1 = (0.1 \times 0.1) + (2 \times 0.1 \times 0.2) + (2 \times 0.1 \times 0.3) = 0.11$$

Now here is where the "RATIO" in Likelihood Ratio comes into play...

$$LR = H_0/H_1$$

$$1/p_1^2 + 2p_1 p_2 + 2p_1 p_3$$

$$1.0/0.11 = 9.09$$

So,

Compared with the prosecution's hypothesis ( $H_0$ ), the defense scenario ( $H_1$ ) is

9-times less well-supported!

Defense hypothesis 2 is a little more involved:

(but then how would YOU explain the victim not being in *her* pantyhose!)

Under the hypothesis  $H_2$  all possible genotype combinations will have to be enumerated

Ind 2	Individual 1					
	(7,7)	(7,8)	(7,9)	(8,8)	(8,9)	(9,9)
(7,7)					.0012	
(7,8)			.0024		.0048	.0036
(7,9)		.0024		.0024	.0072	
(8,8)			.0024			
(8,9)	.0012	.0048	.0072			
(9,9)		.0036				

# How do we get these probabilities?

Each is the probability of getting Genotype A **and** Genotype B

First individual = (7,7)

Second individual = (8,9)

=  $(0.1 \times 0.1) \times (2 \times .2 \times .3)$

=  $0.01 \times 0.12$

= **0.0012**

Ind 2	Individual 1					
	(7,7)	(7,8)	(7,9)	(8,8)	(8,9)	(9,9)
(7,7)					.0012	
(7,8)			.0024		.0048	.0036
(7,9)		.0024		.0024	.0072	
(8,8)			.0024			
(8,9)	.0012	.0048	.0072			
(9,9)		.0036				



Of course...we could incorporate  $\theta$   
here as well:

For homozygotes:  $p^2 + p(1 - p)\theta$

with  $\theta = 0.01$

First individual = (7,7)

Second individual = (8,9)

=  $(0.1^2 + 0.1(1 - 0.1)0.01) \times (2 \times .2 \times .3)$

=  $0.0109 \times 0.12$

= **0.0013**

*or*

Of course...we could incorporate  $\theta$   
here as well:

For homozygotes:  $p^2 + p(1 - p)\theta$

with  $\theta = 0.03$

First individual = (7,7)

Second individual = (8,9)

=  $(0.1^2 + 0.1(1 - 0.1)0.03) \times (2 \times .2 \times .3)$

=  $0.0127 \times 0.12$

= **0.0015**

*Big deal!*

## What next...

The total probability that two unrelated persons explain the mixture alleles (7,8,9) = Sum of probabilities in the enumerated cells :

$$\begin{aligned}\Sigma p &= 0.0012 + 0.0024 + \dots + 0.0036 \\ &= \mathbf{0.0432}\end{aligned}$$

So,

The Defense Hypothesis 2 is:

Approximately 23 times  
less well supported than  
the Prosecution's  
Hypothesis

# HOW TO EXPRESS THE NUMBERS FROM LIKELIHOOD RATIO COMPUTATIONS

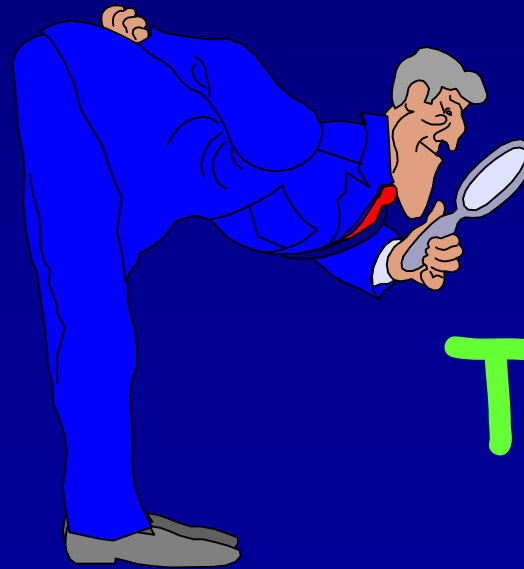
- When making statements on the statistical inferences remember that you are expressing **only the genetic data**
- You are not dealing with issues of “**chance**”
- To do so would involve Bayesian inferences which include Prior Probabilities...for which genetic data offers little assistance.

So, with regard to Defense Hypothesis 1 we could say:

The observed mixture profile is 9-times more likely to occur under the scenario that it is a mixture of DNA from the victim and suspect, as opposed to the scenario that it originated from a mixture of DNA of the victim and an unrelated unknown person.

# Conservative

## Basic



True!

# What this doesn't mean:

With a chance of 1 in 9, an unknown person could have contributed DNA in this mixture

**Wrong!!!**



Or

The probability (chance) that the suspect contributed DNA to this mixture is 1 in 9.

**Wrong Again !!!**

## And with regard to Defense Hypothesis 2 we could say:

The observed mixture profile is 23-times more likely to occur under the scenario that it is a mixture of DNA from the victim and suspect, as opposed to the scenario that it originated from a mixture of DNA from two unrelated, unknown persons.

# Assumptions In Likelihood Computations

Unknown persons are assumed to be **unrelated** in scenarios, as well as unrelated to the known persons whose contributions are proposed in the mixture.

# Assumptions In Likelihood Computations

The different hypotheses of the origin of the mixture assume **prescribed number of contributors** in the mixture.

**Add other potential contributors and you add to the total potential genotypes to be considered**

# Assumptions In Likelihood Computations

All individuals contributing alleles in the mixture are assumed to be of the **same population-origin**, so that the same allele frequencies remain applicable to all of them.

# Assumptions In Likelihood Computations

The population is assumed to be at H-WE, so that genotype frequencies of one or more persons could be computed by the product rule.

Potential subdivision can be addressed by incorporating appropriate  $\theta$  values

## Lets look at a different scenario

Often you may have evidence that presents a mixture and a suspected contributor...

The question would be:

What is the likelihood of the suspect being a contributor to the evidentiary pattern?

**Suspect**

**Evidence**

  $A_1$

  $A_1$

  $A_2$

  $A_2$

  $A_3$

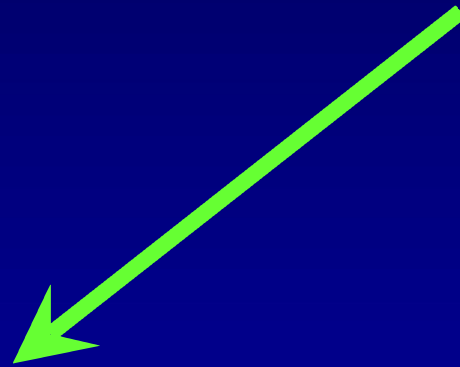
  $A_4$

**Four Allele Scenario**



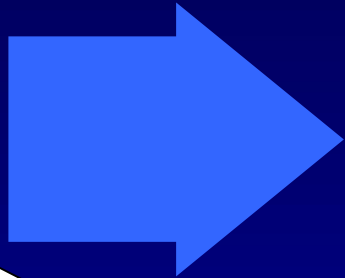
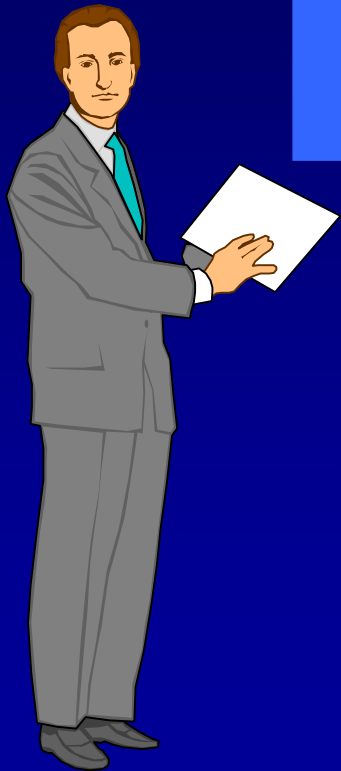
Two alleles match the suspect -  $A_1$  &  $A_2$

Two alleles match the unknown -  $A_3$  &  $A_4$



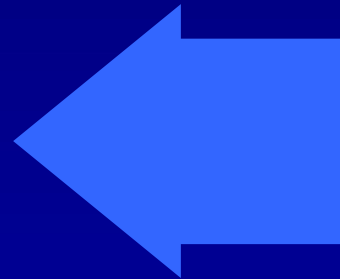
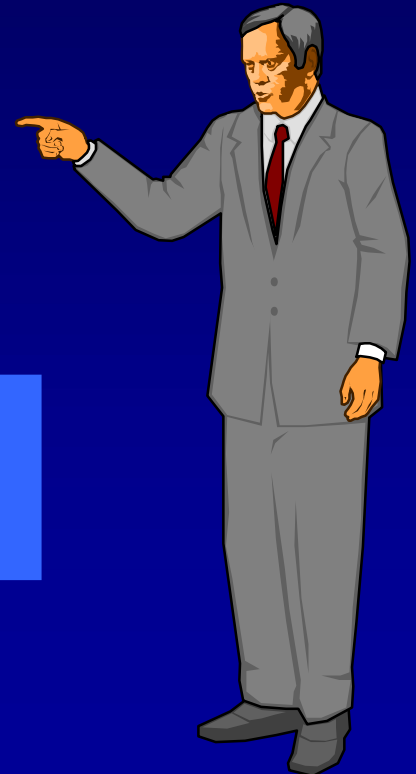
Assuming there is only one  
unknown contributor

# Mutually Exclusive Hypotheses



**Prosecution**

DNA is from suspect  
and unknown



**Defense**

DNA is from two  
unknown persons

The prosecution may postulate that the suspect and an unknown explain all alleles seen in the mixture.

$H_0$ : The mixture originated from the suspect and an unknown individual

Under this hypothesis,

The components of the mixture are **explained** with a probability of

$$1 \times 2p_3p_4$$

Probability of  
the suspect's  
contribution

Probability of  
the unknown's  
contribution

The defense might argue that the following hypothesis should be entertained:

$H_1$ : The mixture originated from two unknown persons

With 4 alleles and 2 contributors the following possible scenarios exist:

Unk 1

$A_1 A_2$

$A_1 A_3$

$A_1 A_4$

$A_2 A_3$

$A_2 A_4$

$A_3 A_4$

Unk 2

$A_3 A_4$

$A_2 A_4$

$A_2 A_3$

$A_1 A_4$

$A_1 A_3$

$A_1 A_2$

$2p_1 p_2 \times 2p_3 p_4$

$2p_1 p_3 \times 2p_2 p_4$

$2p_1 p_4 \times 2p_2 p_3$

$2p_2 p_3 \times 2p_1 p_4$

$2p_2 p_4 \times 2p_1 p_3$

$2p_3 p_4 \times 2p_1 p_2$

---

$24p_1 p_2 p_3 p_4$

**The resulting likelihood ratio is:**

$$\frac{2p_3 p_4}{24p_1 p_2 p_3 p_4} \cdot \frac{1}{12p_1 p_2}$$

So, lets throw some numbers at it..

If  $p_1 = 0.15$  &  $p_2 = 0.2$

$$\frac{1}{12p_1 p_2} = \frac{1}{12(0.15)(0.2)}$$
$$\approx 3$$

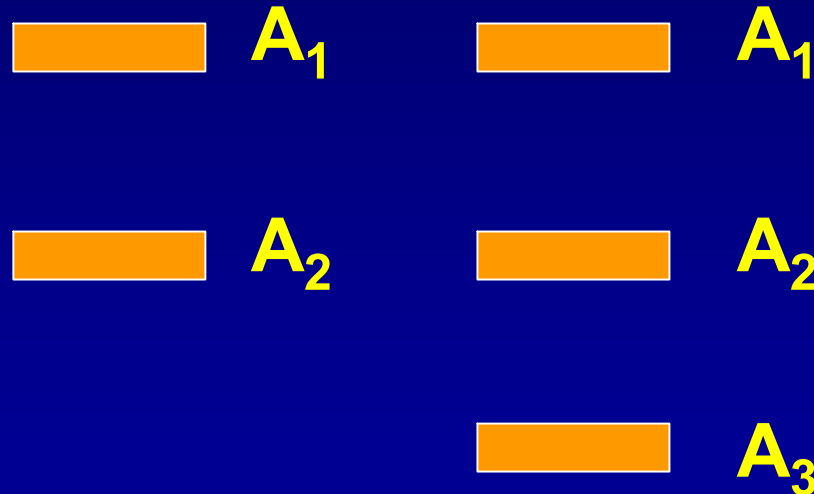


So, with regard to Defense Hypothesis 1 we could say:

The observed mixture profile is approximately **3-times** more likely to occur under the scenario that it is a mixture of DNA from the suspect and an unknown, as opposed to the scenario that it originated from a mixture of DNA of two unrelated unknown persons.

# Now lets really have fun!!

Suspect      Evidence



## Three Allele Scenario

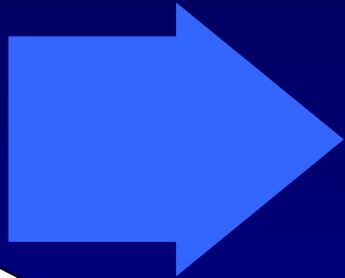
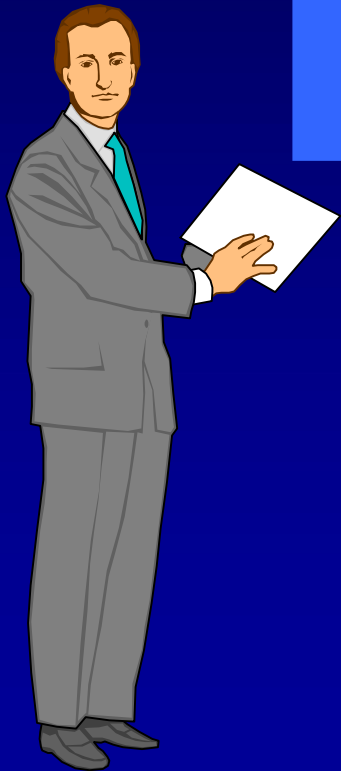
Same question as before but...

## Three Alleles

Two match the suspect -  $A_1A_2$

The unknown contributes - at least  $A_3$

# Mutually Exclusive Hypotheses

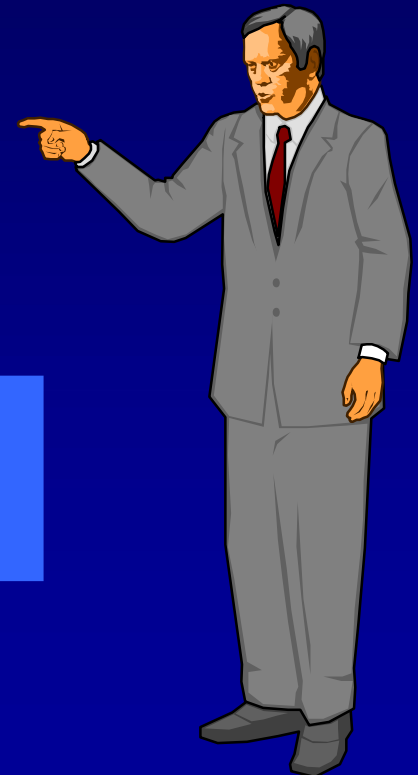
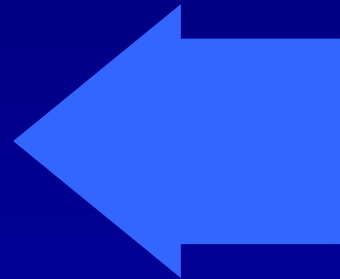


**Prosecution**

DNA is from suspect  
and unknown

**Defense**

DNA is from two  
unknown persons



Under the Prosecution's hypothesis,

The components of the mixture are **explained** with a probability of

$$1 \times \frac{A_3 A_3}{p_3^2} + \frac{A_1 A_3}{2p_1 p_3} + \frac{A_2 A_3}{2p_2 p_3}$$

←  
Probability of  
the suspect's  
contribution

→  
Probability of  
the unknown's  
contribution

Now, the Defense scenario  
becomes interesting...

Since we don't know if the  
"unknown" is homozygous or  
heterozygous...we must cover all  
bases!

Let's see how this pans out...

Unk 1

$A_1 A_2$

$A_1 A_2$

$A_1 A_2$

$A_1 A_3$

$A_1 A_3$

$A_1 A_3$

$A_2 A_3$

$A_2 A_3$

$A_2 A_3$

Unk 2

$A_1 A_3$

$A_2 A_3$

$A_3 A_3$

$A_1 A_2$

$A_2 A_3$

$A_2 A_2$

$A_1 A_2$

$A_1 A_3$

$A_1 A_1$

$2p_1 p_2 \times 2p_1 p_3$

$2p_1 p_2 \times 2p_2 p_3$

$2p_1 p_2 \times p_3^2$

$2p_1 p_3 \times 2p_1 p_2$

$2p_1 p_3 \times 2p_2 p_3$

$2p_1 p_3 \times p_2^2$

$2p_2 p_3 \times 2p_1 p_2$

$2p_2 p_3 \times 2p_1 p_3$

$2p_2 p_3 \times p_1^2$

Not done yet!

$A_1A_1$

$A_2A_3$

$p_3^2 \times 2p_2p_3$

$A_2A_2$

$A_1A_3$

$p_2^2 \times 2p_1p_3$

$A_3A_3$

$A_1A_2$

$p_3^2 \times 2p_1p_2$

---

$$12p_1p_2p_3(p_1 + p_2 + p_3)$$

Did you forget anything???



**The Likelihood Ratio becomes:**

$$p_3^2 + 2p_1 p_3 + 2p_2 p_3$$

---

$$12p_1 p_2 p_3 (p_1 + p_2 + p_3)$$

or

$$p_3 + 2p_1 + 2p_2$$

---

$$12p_1 p_2 (p_1 + p_2 + p_3)$$

So, want to throw some numbers at this...just for a taste?

Using our allele frequencies from before:

Let

$$p_1 = 0.1, p_2 = 0.2, \text{ and } p_3 = 0.3$$

$$p_1 = 0.1, p_2 = 0.2, \text{ and } p_3 = 0.3$$

$$LR = \frac{p_3 + 2p_1 + 2p_2}{12p_1p_2(p_1 + p_2 + p_3)}$$

$$= \frac{0.9}{0.144} = 6.25$$

So,

Compared with the prosecution's hypothesis ( $H_0$ ), the defense scenario ( $H_1$ ) is

6-times less well-supported!

So, with regard to Defense Hypothesis 1 we could say:

The observed mixture profile is approximately **6-times** more likely to occur under the scenario that it is a mixture of DNA from the suspect and an unknown, as opposed to the scenario that it originated from a mixture of DNA of two unrelated unknown persons.

**Now...Let's have some real fun!**

**Scenario:**

***Sexual assault case where a mixture  
was observed on the vaginal swab.***

# Our data:

## Evidentiary Mixture

<u>Locus</u>	<u>Alleles</u>
D3S1358	14, 15, 16, 17
vWA	13, 14, 16, 17, 18, 20
D8S1179	13, 14, 15
D21S11	27, 29, 31, 31.2, 32.2
D18S51	12, 13, 16, 18
D5S818	11, 12, 13
D13S317	8, 9, 11, 12, 13
D7S820	8, 9, 10, 11
D16S539	9, 11, 12, 13
TH01	6, 7, 9, 9.3
TPOX	8, 9, 10
CSF1PO	10, 12, 13
FGA	20, 22, 23, 24

What would you suggest about this mixture??

# Our Knowns:

## Victim Known

<u>Locus</u>	<u>Alleles</u>
D3S1358	14, 15
vWA	13, 18
D8S1179	13, 14
D21S11	27, 31
D18S51	13, 18
D5S818	12, 13
D13S317	9, 11
D7S820	10, 11
D16S539	12
TH01	6, 7
TPOX	8, 10
CSF1PO	10
FGA	22, 24

## Suspect Known

<u>Locus</u>	<u>Alleles</u>
D3S1358	17
vWA	14, 16
D8S1179	13, 15
D21S11	29, 31.2
D18S51	12, 18
D5S818	11, 12
D13S317	8, 12
D7S820	8, 11
D16S539	12, 13
TH01	7, 9.3
TPOX	8, 9
CSF1PO	12, 13
FGA	20, 23

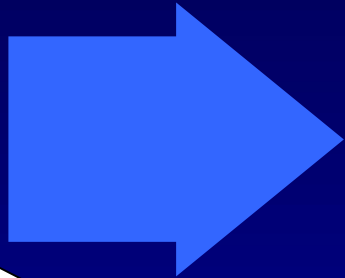
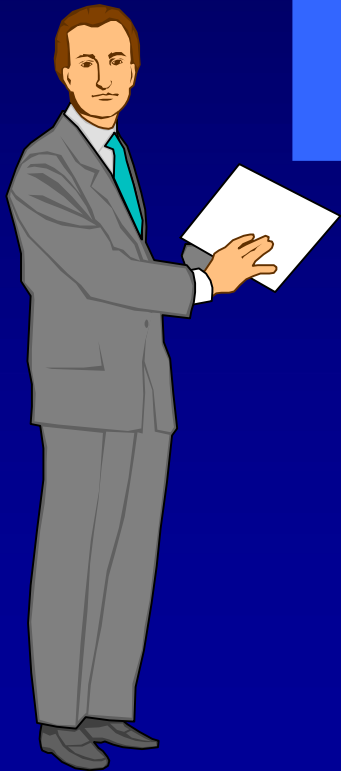
## Consensual Partner Known

<u>Locus</u>	<u>Alleles</u>
D3S1358	16
vWA	17, 20
D8S1179	13
D21S11	29, 32.2
D18S51	13, 16
D5S818	12, 13
D13S317	11, 13
D7S820	9, 10
D16S539	9, 11
TH01	7, 9
TPOX	8, 9
CSF1PO	10
FGA	22

Let's see how this scenario effects the statistics



# Mutually Exclusive Hypotheses

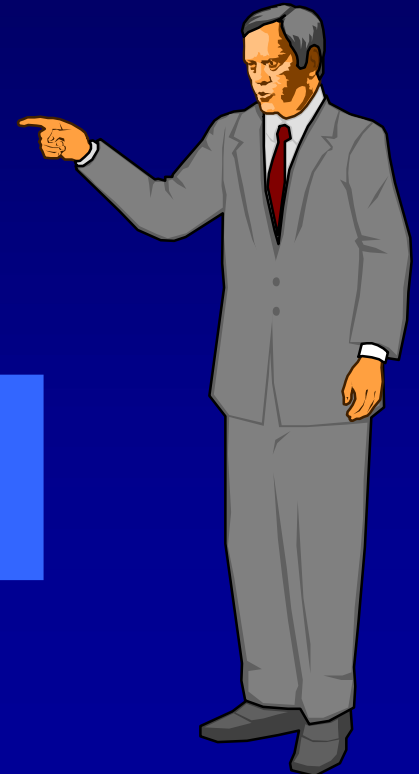
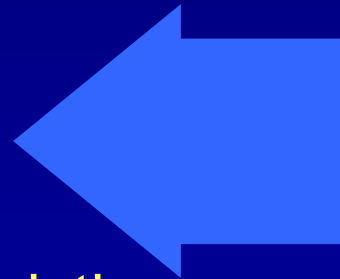


## Prosecution

DNA is from victim, her partner and the suspect

## Defense

DNA is from victim, her partner and an unknown person



$H_0$  = The results are explained by a mixture of DNA derived from the victim, a consensual partner, and the suspect

$H_{a1}$  = The results are explained by a mixture of DNA derived from the victim, a consensual partner, and an unknown individual

So, in this case, the numerator will be 1

It's the denominator values that you need to think about!

Lets look at a few examples:

### **Evidentiary Mixture**

<u>Locus</u>	<u>Alleles</u>
D3S1358	14, 15, 16, 17

D3

Mixture

Victim

Partner

Unknown

14,15,16,17

14,15

16,16

17

Perpetrator could be:

17,17

14,17

15,17

16,17

As long as the hypothesis is based on 3 contributors!

Suspect genotype



At this locus the denominator would be:

$$(17)^2 + 2(14)(17) + 2(15)(17) + 2(16)(17)$$

If we used SW Hispanic allele frequencies:

D3S1358	Hispanic (N=209)
<12	0.000
12	0.000
13	0.239
14	7.895
15	42.584
15.2	0.000
16	26.555
17	12.679
18	8.373
19	1.435
>19	0.239

14 = 0.07895

15 = 0.42584

16 = 0.26555

17 = 0.12679

At this locus the denominator would be:

$$(17)^2 + 2(14)(17) + 2(15)(17) + 2(16)(17)$$

$$(0.12679)^2 + 2(0.07895)(0.12679) + 2(0.42584)(0.12679) + 2(0.26555)(0.12679)$$

$$= 0.21142$$


$$LR = \frac{1}{0.21142} = 4.729$$

The observed mixture profile is approximately **4.5 times** more likely to occur under the scenario that it is a mixture of DNA from the victim, her partner, and the suspect, as opposed to the scenario that it originated from a mixture of DNA from the victim, her partner, and an unrelated, unknown person.

# What about this one?

## Evidentiary Mixture

<u>Locus</u>	<u>Alleles</u>
D3S1358	14, 15, 16, 17
vWA	13, 14, 16, 17, 18, 20



vWA

<u>Mixture</u>	<u>Victim</u>	<u>Partner</u>	<u>Unknown</u>
13, 14, 16, 17, 18, 20	13, 18	17, 20	14, 16

Perpetrator could be:





At this locus the denominator would be:

$$2(14)(16)$$

If we used SW Hispanic allele frequencies:

VWA	Hispanic (N=203)
11	0.246
13	0.000
14	6.158
15	7.635
16	35.961
17	22.167
18	19.458
19	7.143
20	1.232
21	0.000


$$14 = 0.06158$$


$$16 = 0.35961$$

$$2(0.06158)(0.35961)$$

$$= 0.04429$$

$$LR = \frac{1}{0.04429} = 22.57$$

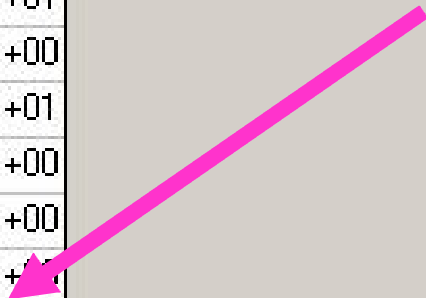
The observed mixture profile is approximately **22.5 times** more likely to occur under the scenario that it is a mixture of DNA from the victim, her partner, and the suspect, as opposed to the scenario that it originated from a mixture of DNA from the victim, her partner, and an unrelated, unknown person.

# Of course, we wouldn't want to do this by hand

## Likelihood Ratio

	CAU	BLK	SEH	SWH
Locus	C1: 0 Unknown	C2: 1 Unknown	Likelihood Ratio	
D3S1358	1.0000E+00	2.1145E-01	4.7293E+00	
VWA	1.0000E+00	4.4303E-02	2.2572E+01	
FGA	1.0000E+00	2.0049E-02	4.9878E+01	
D8S1179	1.0000E+00	1.4575E-01	6.8611E+00	
D21S11	1.0000E+00	8.0045E-02	1.2493E+01	
D18S51	1.0000E+00	8.2697E-02	1.2092E+01	
D5S818	1.0000E+00	5.0317E-01	1.9874E+00	
D13S317	1.0000E+00	2.8834E-02	3.4681E+01	
D7S820	1.0000E+00	1.3590E-01	7.3584E+00	
CSF1PO	1.0000E+00	5.0685E-02	1.9730E+01	
TPOX	1.0000E+00	3.8688E-01	2.5848E+00	
TH01	1.0000E+00	3.8323E-01	2.6094E+00	
D16S539	1.0000E+00	1.5138E-01	6.6059E+00	
Total	1.000E+00	4.064E-13	2.461E+12	

What does this mean?



# Big Number Names:

•	1,000,000	million
•	1,000,000,000	billion
•	1,000,000,000,000	trillion
•	$1 \times 10^{15}$	quadrillion
•	$1 \times 10^{18}$	quintillion
•	$1 \times 10^{21}$	sextillion
•	$1 \times 10^{24}$	septillion
•	$1 \times 10^{27}$	octillion
•	$1 \times 10^{30}$	nonillion
•	$1 \times 10^{33}$	decillion

The observed mixture profile is approximately **2.5 trillion times** more likely to occur under the scenario that it is a mixture of DNA from the victim, her partner, and the suspect, as opposed to the scenario that it originated from a mixture of DNA from the victim, her partner, and an unrelated, unknown person.

# Considerations

Mixture interpretation, and the statistical treatment of the data, is more complex than interpretation of evidence originated from a single donor. However, **with appropriate care**, the same biological and statistical principles can be used in mixture interpretation.

# Considerations

Unlike interpretation of single donor profiles, the relevant **questions** for mixture interpretation **can be varied**, and a wider set of scenarios with respect to the origin of the mixture may be postulated...each hypothesis is mutually exclusive and applies a different treatment of the data

# Considerations

As with the interpretation of single donor profiles, conservative approaches for calculating statistics of mixture interpretation should be made.

However, when applying the likelihood ratio approach, population substructure adjustments **do not** always yield conservatism.



# Considerations

Subtraction of alleles found in the known samples from the mixture **should be avoided** in deriving statistics for mixture interpretation.

This adds to conservatism, even with the use of the simplest assumption in calculations.

# Considerations

Several biological features of mixture profiles may be relatively difficult to translate in formulating statistics.

However, when they are not factors in the analysis, the derived statistics become inherently conservative.

# Considerations

**Most critical** step of a mixture interpretation is how the statistics is **verbally presented**.

A LR-value, wrongly stated, may introduce the fallacy of reverse conditioning, sometimes known as the '**prosecutors fallacy**'.

Had Enough PPP

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